

# Contrastive Ranking-Aware Learning

## CoRAL – Decoupled Representations for Retrieval



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# Background

## Overview on Approaches

### **Generic Retrieval Model**

“Given a query, (*Representations*) induce a (*Relevance Estimation*), which orders (*Identifiers*) that map to (*Results*). ”

# Background

## Overview on Approaches

### BM25

“Given a query, *sparse representations* induce a *lexical matching*, which orders *doc IDs* that map to *documents*. ”

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#### Traditional

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|                         |               |
|-------------------------|---------------|
| Example                 | BM25          |
| <i>Representations</i>  | Sparse Repr.  |
| <i>Relevance Estim.</i> | Lexical Match |
| <i>Identifiers</i>      | Doc-IDs       |
| <i>Results</i>          | Documents     |

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# Background

## Overview on Approaches

### Bi-Encoder

“Given a query, *dense representations* induce an *inner product space*, which orders *doc IDs* that map to *documents*. ”

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|                         | <b>Traditional</b> | <b>Neural</b>     |
|-------------------------|--------------------|-------------------|
|                         |                    | Representation L. |
| Example                 | BM25               | Bi-Encoder [5]    |
| <i>Representations</i>  | Sparse Repr.       | Dense Repr.       |
| <i>Relevance Estim.</i> | Lexical Match      | Inner Product Sp. |
| <i>Identifiers</i>      | Doc-IDs            | Doc-IDs           |
| <i>Results</i>          | Documents          | Documents         |

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# Background

## Overview on Approaches

### Cross-Encoder

“Given a query, *directly* order *doc IDs* that map to *documents*. ”

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|                         | <b>Traditional</b> | <b>Neural</b>     |                   |
|-------------------------|--------------------|-------------------|-------------------|
|                         |                    | RepresentationL.  | Metric Learning   |
| Example                 | BM25               | Bi-Encoder [5]    | Cross-Encoder [5] |
| <i>Representations</i>  | Sparse Repr.       | Dense Repr.       | –                 |
| <i>Relevance Estim.</i> | Lexical Match      | Inner Product Sp. | Direct            |
| <i>Identifiers</i>      | Doc-IDs            | Doc-IDs           | Doc-IDs           |
| <i>Results</i>          | Documents          | Documents         | Documents         |

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# Background

## Overview on Approaches

### Differentiable Index

“Given a query, *generate doc IDs* that map to *documents*. ”

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|                         | <b>Traditional</b> | <b>Neural</b>     |                   |                  |
|-------------------------|--------------------|-------------------|-------------------|------------------|
|                         |                    | RepresentationL.  | Metric Learning   | “Index Learning” |
| Example                 | BM25               | Bi-Encoder [5]    | Cross-Encoder [5] | Diff. Index [6]  |
| <i>Representations</i>  | Sparse Repr.       | Dense Repr.       | –                 | –                |
| <i>Relevance Estim.</i> | Lexical Match      | Inner Product Sp. | Direct            | –                |
| <i>Identifiers</i>      | Doc-IDs            | Doc-IDs           | Doc-IDs           | Gen. Doc-IDs     |
| <i>Results</i>          | Documents          | Documents         | Documents         | Documents        |

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# Background

## Overview on Approaches

### Infinite Index

“Given a query, *generate documents.*”

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|                         | <b>Traditional</b> | <b>Neural</b>     |                   |                  |                    |
|-------------------------|--------------------|-------------------|-------------------|------------------|--------------------|
|                         |                    | RepresentationL.  | Metric Learning   | “Index Learning” | “Generative L.”    |
| Example                 | BM25               | Bi-Encoder [5]    | Cross-Encoder [5] | Diff. Index [6]  | Infinite Index [1] |
| <i>Representations</i>  | Sparse Repr.       | Dense Repr.       | –                 | –                | –                  |
| <i>Relevance Estim.</i> | Lexical Match      | Inner Product Sp. | Direct            | –                | –                  |
| <i>Identifiers</i>      | Doc-IDs            | Doc-IDs           | Doc-IDs           | Gen. Doc-IDs     | –                  |
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Efficiency





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| Efficiency              |                    |                   |                   |                  |                    |
| Effectiveness           |                    |                   |                   |                  |                    |

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| Efficiency              |               |                   |                   |                  |                    |
| Effectiveness           |               |                   |                   |                  |                    |

Bi-Encoders offer a good tradeoff between efficiency and effectiveness.

# Motivation

## Problems of Bi-Encoders

Current Bi-Encoders are subject to three problems:

### 1. Task discrepancy

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- Inference: multiple positives with graded relevance

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- This training setup is mostly due to sparsity of ground truth labels

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**Contribution:** knowledge distillation with graded, single-query batches

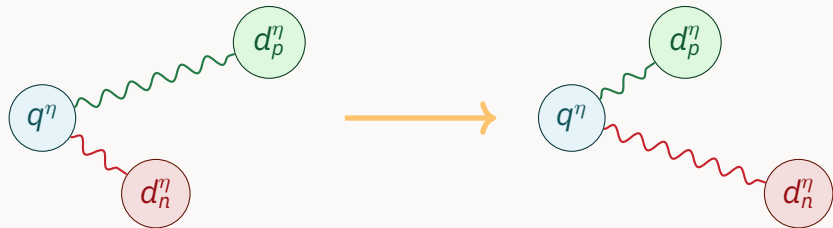


## **(I) Fixing Task Discrepancy**

# Model Architecture

## Contrastive Learning

**Objective:** given an anchor (query  $q$ ) and a positive (document  $d_p$ ) and negative (document  $d_n$ ) example, minimize the distance between anchor and positive and maximize the distance between anchor and negative.



Contrastive learning can be extended to multiple positives and negatives.  
**But:** does not discriminate in-class (i.e., trains set retrieval only).

# Model Architecture

## Contrastive Ranking-Aware Learning

Ranking information can be directly integrated into the loss [2, 7]:

$$l_{\tau,k}(q, D) = \log \frac{\exp(q^\eta \cdot d_i^\eta / \tau)}{\sum_{j=1}^b \exp(q^\eta \cdot d_j^\eta / \tau)}$$

For each query  $q$ ...

... using a standard **contrastive loss**

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- ... is contrasted by each **document following it** (negatives).

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Standard BERT-based text encoders are used for  $\eta_q$  and  $\eta_d$ .

# Model Architecture

## Contrastive Ranking-Aware Learning

$$\sum_{i=3}^k$$

$d_{14}$   $d_1$   $d_{27}$   $d_5$   $d_9$   $d_{12}$   $d_{127}$   $d_{62}$   $d_{49}$   $d_{45}$

For example, at **iteration 3** of the loss computation ...

... with a batch of 10 documents from  $D$ ,



# Model Architecture

## Contrastive Ranking-Aware Learning

$$\sum_{i=3}^k \begin{matrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 \\ d_{14} & d_1 & d_{27} & d_5 & d_9 & d_{12} & d_{127} & d_{62} & d_{49} & d_{45} \end{matrix}$$

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- ... the document at **rank 3 is treated as positive**,
- ... and is contrasted by documents at **ranks 4... $b$  as negatives**.

Analogously, at **iteration 4**, ranks 1, 2, 3 are ignored,  
**rank 4** is treated positive, and **ranks 5... $b$**  as negatives.

# Model Architecture

## Loss Properties

The loss requires the model to learn a latent space such that:

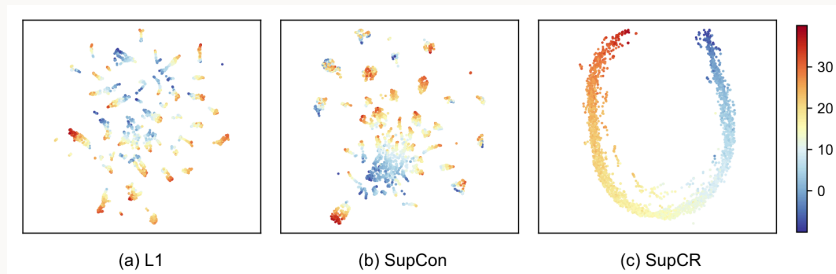
- (1)** maximize similarity of query to positive documents ( $q^n \cdot d_p^n \gg 0$ )
- (2)** minimize similarity sum of query to negative documents ( $\sum q^n \cdot d_n^n \rightarrow 0$ )
- (3)** (1) and (2) are competing because of ranking supervision
  - each negative sample up to  $k$  becomes positive in a later iteration
  - thus (1) and (2) need to balance out between iterations dependent on rank
  - the earlier in the ranking, the more important (1) is over (2) for loss minimum

The global loss is the average over all top- $k$  ranks over all queries.

# Model Architecture

## Summary

In summary, the proposed **CoRAL** loss resembles the target task of retrieval task more closely than previous contrastive pretraining approaches.

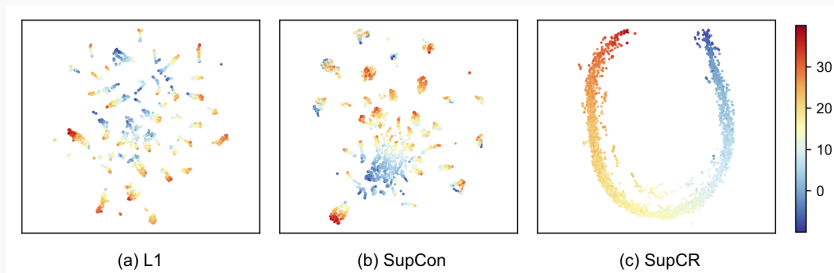


**Figure 1:** UMAP representation of latent space from models trained with L1, InfoNCE, and Ranked Contrastive Loss for temperature classification from webcam images [7].

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**Figure 1:** UMAP representation of latent space from models trained with L1, InfoNCE, and Ranked Contrastive Loss for temperature classification from webcam images [7].

## Contribution

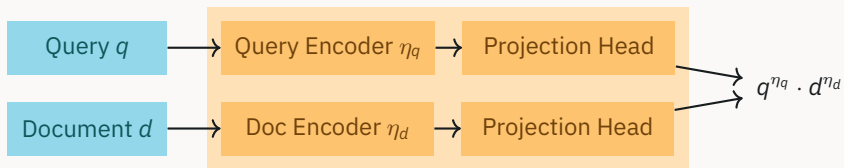
Ranked contrastive loss has only been applied for single target rank concepts; application to multi-faceted rank objectives (retrieval) is novel.



## **(II) Fixing Domain Discrepancy**

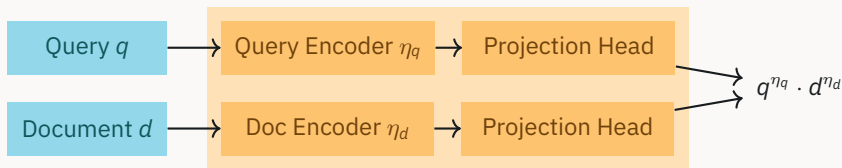
# Decoupled Representations

## Multimodal Training



# Decoupled Representations

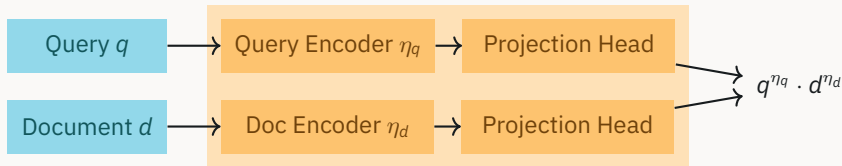
## Multimodal Training



- **Query encoder** can be small & fast for efficiency
- **Document encoder** can be large & complex for effectiveness
- **Multimodal training** with projection heads allows for joint latent space

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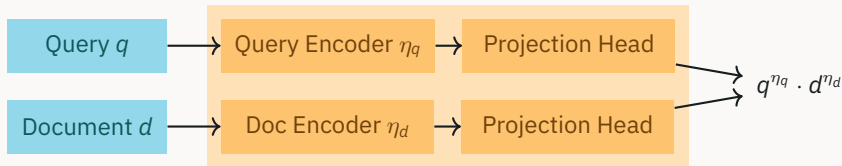


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We can even omit the projection head of the query encoder and utilize a freezed pre-trained model (e.x. distilBERT).

# Decoupled Representations

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## Contribution

Utilize multimodal training to derive both efficient and effective bi-encoder models, taking inspiration from recent multimodal text/image models.

### **(III) Fixing Scale Discrepancy**

# Training Setup

## Batch Construction

### Traditional Setup

- Construct batch from  $(q, d)$  positive pairs; documents from other queries are treated as implicit negatives
- Problem: we can not ensure 'correct' negatives; we only learn top-1 retrieval

### Improved Setup

- Single-query batches based on rank supervision
- Rank supervision induced by an oracle  $\Omega$  (teacher model, ground truth, ...)
- Top- $k$  are used as positives, rest of ranking as negatives

# Training Setup

## Sources of Rank Supervision

- Synthetic rankings from teacher models (e.x. monoT5/duoT5 [3])
  - infinitely available since it can be synthesized at training time
  - but: trained model cannot exceed the effectiveness of the teacher model
- Direct rankings from human annotations (e.x. TREC)
  - sparse, and not suitable for training; evaluation only
- Pseudo rankings from large-scale query-logs (e.x. AQL [4])
  - allows for generalization beyond teacher model
  - vast amount of queries, but: limited depth per query

## Idea

Can we generate training data by combining “real” results from query logs and augment with “synthetic” results from teacher models?



# Current Status

## Done

- Literature review, theoretical foundation
- Model implementation
- Convergence tested on small toy data

## In progress

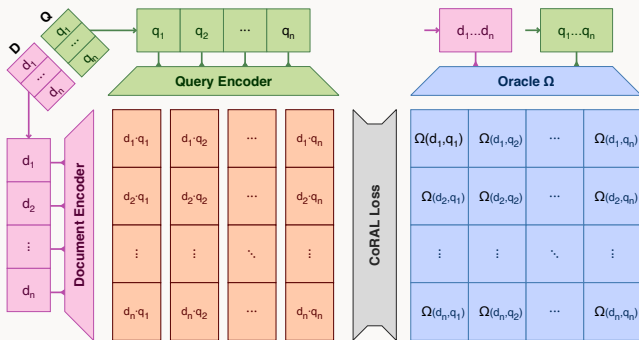
- Data curation & pretrained model selection
- Code optimization for large-scale training

## Todo

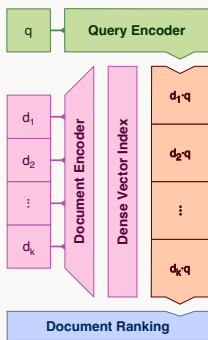
- Batch sampling & training
- Ablation studies & evaluation

# Conclusion

## Training



## Retrieval



## Summary

We address the three main challenges of representation learning for retrieval using a ranked contrastive loss in conjunction with decoupled encoders and knowledge distillation for data augmentation.

# References I

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## References III

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