Exercise 1 : Perceptron Learning

In this exercise, you design a single perceptron with two inputs x_1 and x_2 . This perceptron shall implement the boolean formula $A \wedge \neg B$ with a suitable function $y(x_1, x_2)$. Use the values 0 for *false* and 1 for *true*.

- (a) Draw all possible examples and a suitable decision boundary in a coordinate system.
- (b) Draw the graph of the perceptron. The schematic must include x_1, x_2 , and all model weights.
- (c) Manually determine a set of suitable weights $\mathbf{w} = (w_0, w_1, w_2)$ from your drawings.

Exercise 2 : Perceptron Learning

Why can the boolean formula A XOR B not be learned by a single perceptron? Justify your answer with a drawing.

Exercise 3 : Parameters of the Multilayer Perceptrons

In this exercise, you analyze the number of weights (parameters) of multilayer perceptrons. We use the notation from the lecture (e.g., slide <u>ML:IV-104</u>), where multilayer perceptrons have d layers, p attributes, hidden layer i with l_i units, and an output layer with k units.

- (a) Let d = 4, p = 7, $l_1 = 5$, $l_2 = 3$, $l_3 = 3$, and k = 4. Draw the graph of the multilayer perceptron.
- (b) Calculate the number of weights in the multilayer perceptron of (a).
- (c) Calculate the number of weights in the multilayer perceptron of (a) but with each l_i doubled, i.e., $l_1 = 10, l_2 = 6, l_3 = 6$. Has the number of weights doubled as well?
- (d) Let $f(p, l_1, ..., l_{d-1}, k)$ be a function that computes the number of weights in the general case. Write down an expression for f.